

## Mixing Characteristics of Liquid Phase in an Unbaffled Vessel Agitated by Unsteadily Forward-Reverse Rotating Multiple Impellers

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**Abstract**— Mixing characteristics of liquid phase in an unbaffled vessel containing water with a liquid height-to-diameter ratio of 2 agitated by unsteadily forward-reverse rotating multiple impellers, a cross type of impellers with four delta blades (CDs), were experimentally studied in comparison with that in a baffled vessel agitated by steadily unidirectionally rotating disk turbine impellers with six flat blades (DTs). For the forward-reverse as well as unidirectional modes of operation, the mixing time in multiple impeller system was larger than that in single impeller system with a liquid height-to-diameter ratio of 1. The ratio of mixing time in multiple impeller system to that in single impeller system was small for the forward-reverse agitation mode compared with that for the unidirectional agitation mode. The result was discussed in relation to the difference in bulk flow pattern between the unbaffled vessel with forward-reverse rotating CDs and the baffled vessel with unidirectionally rotating DTs.

**Keywords**— mixing time; unbaffled agitation vessel; unsteadily forward-reverse rotating impeller; multiple impeller system; bulk flow pattern

### I. INTRODUCTION

In industrial agitation operations, deep vessels with multiple impellers characterized by a liquid height-to-diameter ratio larger than unity are frequently employed for practical purposes to get high volumetric mixing and to reduce the floor area occupied by the equipment in the factory. For such a system, it is well known the importance of the impeller design and the determination of impeller arrangement (Nishikawa *et al.*, 1976; Hudcova *et al.*, 1989; Armenante and Chang, 1998; Armenante *et al.*, 1999). For conventional baffled vessels having steadily unidirectionally rotating multiple impellers, the impellers have been arranged on the shaft with the clearance and number determined on the basis of the data on their power consumption. However, whether or not design of the multiple impeller vessel is reasonable in view of operational characteristics is uncertain.

A primary way to investigate the feasibility of design for the multiple impeller vessel is to evaluate the

mixing time of liquid phase which is a fundamental parameter needed not only for homogenization operation of liquid phase but also for mass transfer operation treating dispersions such as gas-liquid mixtures and solid-liquid mixtures. It seems that the results of few studies on the mixing time in baffled vessels having unidirectionally rotating multiple impellers (Komori and Murakami, 1988; Cronin *et al.*, 1994; Jahoda and Machon, 1994; Vasconcelos *et al.*, 1995) have been used as data for design and operation.

Previously, we proposed an unbaffled vessel having unsteadily forward-reverse rotating multiple impellers, a cross type of impellers with four delta blades (CDs), whose rotation reverses its direction periodically, and this type of agitator was named "AJITER" (Yoshida *et al.*, 1996). For CDs in AJITER, the effect of clearance on the power consumption of impellers was elucidated, which is basic for design of the multiple impeller vessel (Yoshida *et al.*, 2002). In order to provide a more sound and generalized basis for design and operation of AJITER, in addition to clarification of the power characteristics of impellers, further study on the mixing characteristics of liquid phase in a vessel is necessary. In this work, the way of arrangement of CDs in multiple fashion was first established, based on the dependence of power consumption on the clearance of forward-reverse rotating multiple CDs in an unbaffled vessel. For the vessel constructed, the effect of the number of impellers on the mixing time was then evaluated experimentally in comparison to that for a baffled vessel having unidirectionally rotating disk turbine impellers (DTs).

### II. METHODS

As the forward-reverse rotating impeller, a cross type impellers with four delta blades (CDs), 120-240 mm in diameter ( $D_i$ ), were employed for an unbaffled vessel. A conventional impeller consisting of a disk turbine impeller with six flat blades (DT), was adopted as the unidirectionally rotating impeller. DTs, 90-150 mm in  $D_i$ , were used under the fully baffled condition (four baffles, 0.1-fold inner diameter of vessel in width). A schematic diagram of the experimental set-up

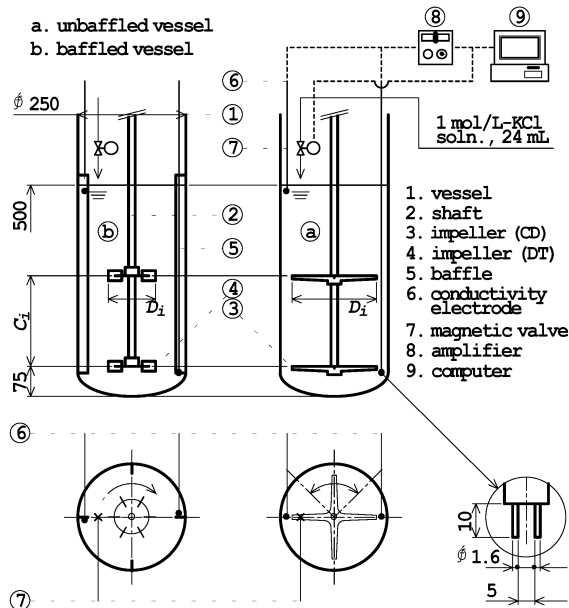


Fig. 1: Schematic flow diagram of experimental apparatus. Dimensions in mm.

is shown in Fig. 1. The vessel of 250 mm inner diameter,  $D_b$ , was used. The depth of liquid,  $H$ , was held at twice  $D_i$  (500 mm). The geometrical conditions such as  $D_i$  and  $H$  were common to the forward-reverse and unidirectional modes of operation, except for the use of the unbaffled or baffled vessel. The distance from the bottom of the lowest impeller,  $C_b$ , was 75 mm. The distance between the impellers on the shaft,  $C_i$ , varied in multiple impeller configuration, ranging from  $0.1D_i$  to  $1.8D_i$ . The average rotation rate of the forward-reverse rotating impeller and the rotation rate of the unidirectionally rotating impeller,  $N_r$ , ranged from 50 to 350 rpm. Control experiments in single impeller configurations for the respective agitation modes were performed under the condition of  $H=D_i$  (250 mm) and  $C_b=75$  mm. For all experiments, deionized water was used at 298 K.

The power consumption of the impellers,  $P_m$ , was determined by measuring the torque with the strain gauges fitted on the shaft. While the power consumption of the impellers in the unidirectional agitation mode is independent of time, that in the forward-reverse agitation mode is unsteady due to periodical change in the impeller rotation rate and that in the shaft torque. In the latter mode of operation, the time-weighted average values over one cyclic time of forward-reverse rotation were employed as  $P_m$ . The power number,  $N_p$ , of unidirectionally rotating impellers is defined by the following equation:

$$N_p = P_m / \rho N_r^3 D_i^5 \quad (1)$$

For the forward-reverse rotating impellers,  $N_p$  was calculated using the average values as the time-dependent variables on the right side of Eqn (1),  $P_m$  and  $N_r$ , respectively.

Batch mixing time of liquid phase was determined

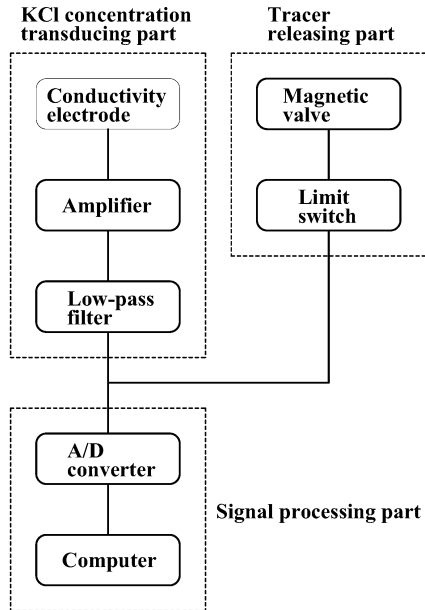


Fig. 2: Block diagram of KCl concentration measuring system.

using a tracer technique (Kramers *et al.*, 1953; Kamiwano *et al.*, 1967). The concentration fluctuation of 0.001-fold liquid volume of passive tracer (1 mol/L, KCl aqueous solution) was examined as a function of time from its rapid release into liquid agitated at the measured  $N_r$ . The concentration fluctuation was evaluated by measuring the difference in electrical conductivity of liquid between the two positions with the platinum wire-made electrode cells (Fig. 1) placed opposite one another near the vessel wall. The two electrode cells were put in a bridge using the electricity supplied as alternating current. The tracer liquid was fed from above the free surface at a position near the upper cell by a small magnetic valve connected with a limit switch. The arrangement of the electrode cells and magnetic valve in the multiple impeller vessel were shown in Fig. 1. For single impeller systems ( $H=250$  mm), the distance between the upper cell and liquid surface, and the distance between the lower cell and vessel bottom were the same as those for multiple impeller systems ( $H=500$  mm). A block diagram of the concentration measuring system is shown in Fig. 2. At the same time as the tracer liquid was released, the data processing system operated by the limit switch recorded the output voltage from the bridge circuit corresponding to the difference in electrical conductivity, i.e., concentration of KCl (Fig. 3). The mixing time,  $T_m$ , was defined as the time from the release of the tracer liquid until the fluctuation was within 5 % of the maximum value of voltage (Shiue and Wong, 1984; Yahata *et al.*, 1985). Moreover, although there was a density difference of about 7 % between liquid within the vessel and tracer liquid, it was ascertained beforehand that mixing due to natural convection could be neglected under the experimental conditions used.

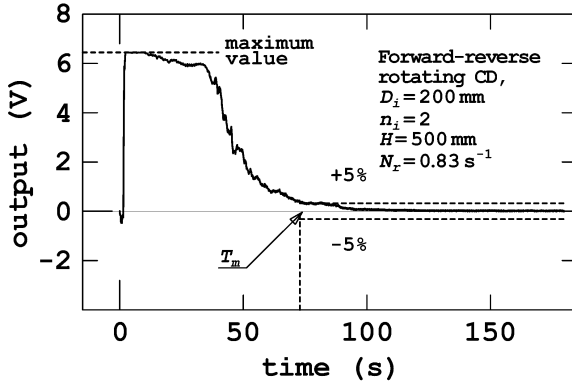


Fig. 3: Time-course of output.

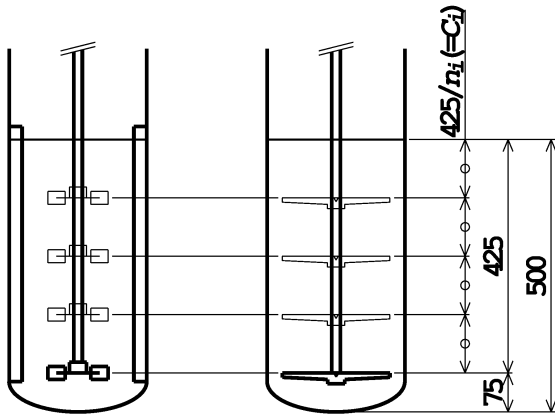


Fig. 4: Arrangement of impellers in multi-stage fashion. Dimensions in mm.

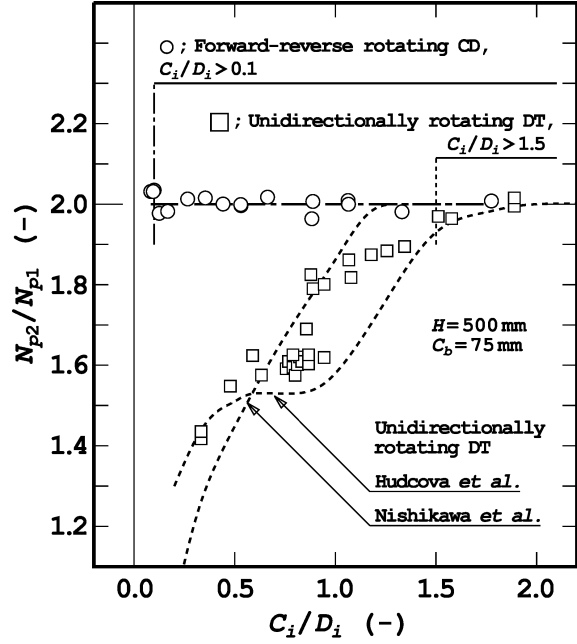
### III. RESULTS AND DISCUSSION

#### A. Arrangement of Impellers in Multiple Impeller System

Based on the power characteristics of the multiple impellers such as forward-reverse rotating CDs and unidirectionally rotating DTs, shown in previous work (Yoshida *et al.*, 2002), the way of arrangement of the impellers in multiple fashion was first established. The distance from the bottom of the lowest impeller,  $C_b$ , was fixed at 75 mm. The impellers were set equidistantly on the shaft in its section (425 mm in distance) between the lowest impeller and liquid surface (see Fig. 4). So, there is the following relation between the number of impellers,  $n_i$ , and the clearance of impellers,  $C_i$ :

$$n_i = 425/C_i \quad (2)$$

The power consumption of multiple impellers changes depending on their clearance. This effect can be described in terms of the differences in the ratio of power number for multiple impellers,  $N_{pn}$ , compared to that for single impeller,  $N_{p1}$ , varying the impeller clearance. When  $N_{pn}/N_{p1} = n_i$ , the impellers on the shaft are regarded to act independently of each other without impeller-impeller flow pattern interaction (Hudcova *et*


Fig. 5: Relationship between  $N_{p2}$  and  $C_i$ 

*al.*, 1989). Arrangement of the impellers with such clearance has the advantage of design due to ability to estimate simply the power consumption and a higher efficiency of energy transmission to fluid (Mochizuki, 1992). The condition on the impeller clearance where  $N_{pn}/N_{p1} = n_i$  was found out on the basis of the data in dual impeller system that is most fundamental among multiple impeller systems. The range of the number of impellers satisfying such condition was then determined. Figure 5 shows the relationship between the power number ratio for dual impellers,  $N_{p2}/N_{p1}$ , and the impeller clearance,  $C_i$ . In the figure,  $C_i$  is divided by the impeller diameter,  $D_i$ . According to the results shown in the figure, when unidirectionally rotating DTs are used in the baffled vessel, the system with values of the specific impeller clearance,  $C_i/D_i$ , ranged above about 1.5 satisfies the condition where the power number ratio,  $N_{p2}/N_{p1}$ , is equal to 2. For respective  $D_i$ s, based on the ranges of  $C_i$ , the ranges of  $n_i$  were determined from Eqn (2). These are listed in Table 1. In the experiment, for reference, DTs were used in the range of  $n_i$  up to four. For forward-reverse rotating CDs in the unbaffled vessel, the experimental result that  $N_{p2}/N_{p1}$  is equal to 2 in the range of  $C_i/D_i$  above 0.1 suggests use of about 20 impellers. In this work, taking practical design into consideration, CDs were used in the range of  $n_i$  from two to eight.

For the number of impellers shown in Table 1, their power consumptions were evaluated in terms of the power number. For any mode of operation, the power number remained almost constant when the impeller rotation rate was varied. This suggests that the flow generated by forward-reverse rotating CDs and that generated by unidirectionally rotating DTs are in turbulent regime. Figure 6 shows the relationship between

Table 1. Determination of the number of impeller stages based on the power consumption.

Agitation mode	$D_i$ (mm)	$C_i/D_i$ (-)	$C_i$ (mm)	$n_i$ (-)
Unidirectionally	90		>135	<3
	120	>1.5	>180	<2
	150		>225	<2
Forward-reverse	120		>12	<35
	160	>0.1	>16	<27
	200		>20	<21
	240		>24	<18

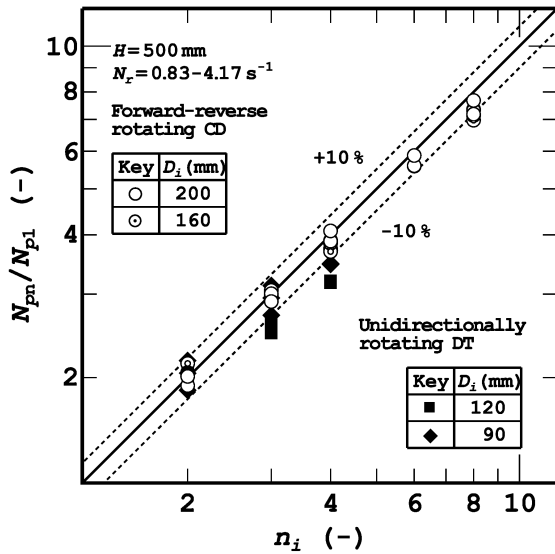


Fig. 6: Relationship between  $N_{pn}$  and  $N_i$ .

the power number ratio for multiple impellers,  $N_{pn}/N_{p1}$ , and the number of impellers,  $n_i$ . The solid line in the figure represents that  $N_{pn}/N_{p1}=n_i$ . The values of  $N_{pn}/N_{p1}$  for forward-reverse rotating CDs agreed with  $n_i$  within approximately 10 %. In the unidirectional agitation mode,  $N_{pn}/N_{p1}$  for triple DTs and that for fourfold DTs exhibited the values smaller than the corresponding  $n_i$ s, 3 and 4, respectively, reflecting decrease of the power number with decrease of the impeller clearance as shown in Fig. 5. These support the above predictive results of the power consumption of multiple impellers on the basis of the data in dual impeller system.

**B. Mixing Time**

The mixing characteristics of liquid phase were then examined for the multiple impeller systems. Evaluation was first made for dual impeller system where the above-mentioned condition based on the power consumption is satisfied in common. Figure 7 shows the effect of impeller rotation rate,  $N_r$ , on the mixing time in dual impeller system,  $T_{m2}$ , for the unbaffled vessel with forward-reverse rotating CDs and the baffled vessel with unidirectionally rotating DTs, respectively. In the figure, the values of mixing time in single impeller system,  $T_{m1}$ , were also plotted for comparison. For both the

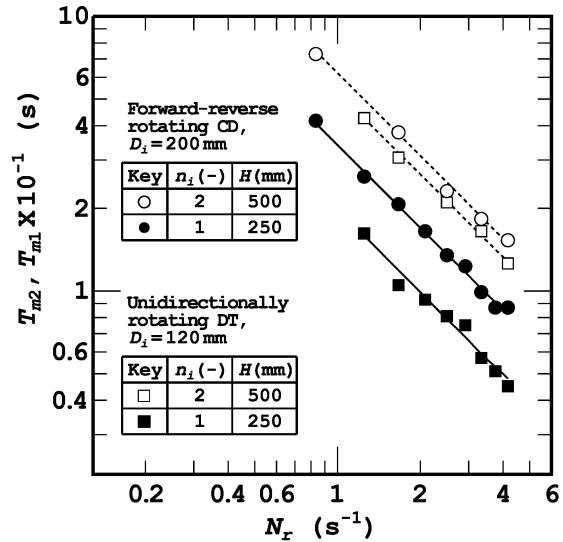


Fig. 7: Relationship between  $T_m$  and  $N_r$ .

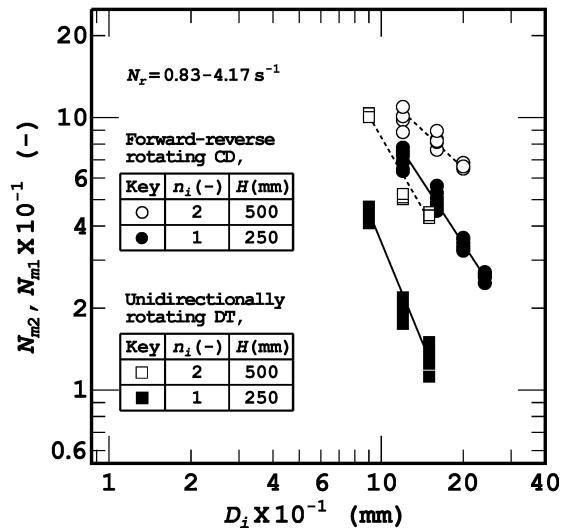


Fig. 8: Relationship between  $N_m$  and  $D_i$ .

modes of operation,  $T_{m2}$  decreased with increase of  $N_r$ , and there was an inverse relation between  $T_{m2}$  and  $N_r$  (Nienow, 1997). That is, the dimensionless mixing time,  $N_m$ , that is the product of the mixing time and impeller rotation rate was almost independent of  $N_r$ . For the difference between the dual and single impeller systems, the tendency that  $T_{m2}$  was on the whole larger than  $T_{m1}$  was common to the two agitation modes. It was also found that the rate of increase of the mixing time due to increase of the liquid depth was small for the forward-reverse agitation mode compared with that for the unidirectional agitation mode. Figure 8 shows the results of the dimensionless mixing time in dual impeller system,  $N_{m2}$ , and that in single impeller system,  $N_{m1}$ , with variation of the impeller diameter,  $D_i$ , respectively.  $N_{m2}$  and  $N_{m1}$  tended to decrease with increasing  $D_i$ , but the rate of decreasing differed between the dual and single impeller systems. That is, the dependence of  $N_{m2}$  on  $D_i$  was small compared to that of  $N_{m1}$ . This difference

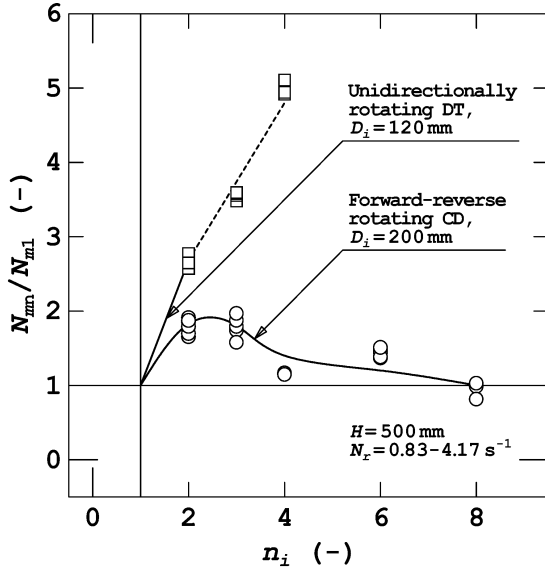


Figure 9. Relationship between  $N_{mm}$  and  $n_i$ .

suggests that increasing the impeller diameter is not sufficiently effective for decreasing the mixing time in the deep vessel. The mixing characteristics in the deep vessel are significantly affected by the liquid flow between the upper and lower regions within the vessel (Komori and Murakami, 1988; Jahoda and Machon, 1994). In view of this, design taking into consideration the geometry in the axial direction seems reasonable. In other words, for decreased mixing characteristics, by increasing the number of impellers, some improvement may be expected.

Evaluations for the systems where the number of impellers was further increased were then made. Figure 9 shows the relationship between the ratio of dimensionless mixing time in multiple impeller system to that in single impeller system,  $N_{mm}/N_{m1}$ , and the number of impellers,  $n_i$ . The impeller clearances in the baffled vessel with unidirectionally rotating triple DTs and that with unidirectionally rotating fourfold DTs are in range where the impellers on the shaft are regarded to act interferingly with each other, with impeller-impeller flow pattern interaction, affecting the power consumption. Under the conditions shown with the dotted line in the figure, further increasing of the mixing time compared to that in dual DT system was observed. On the other hand, it was found that the mixing time in the unbaffled vessel with forward-reverse rotating multiple CDs tended to decrease with increasing  $n_i$ .

The difference in the dependence of mixing time on the number of impellers suggests the difference in the bulk flow pattern within the vessel between the modes of operation. A decreasing of the mixing time is perceived to be due to an increasing of the axial component in the bulk flow to provide larger scale circulating flow field with more whole mixing throughout the vessel. In previous work (Yoshida *et al.*, 2002), it was illustrated that the discharge flow from forward-reverse rotating

CD has larger axial component and that the use of impellers in multiple fashion results in a series of discharge flows between the adjacent impellers. The main cause for an improved mixing characteristics of the unbaffled vessel with forward-reverse rotating multiple CDs, namely tendency for the mixing time to decrease with the number of impellers, may be a reflection of the bulk flow with larger axial component.

#### IV. CONCLUSIONS

Mixing characteristics of liquid phase in an unbaffled vessel containing water with a liquid height-to-diameter ratio of 2 agitated by unsteadily forward-reverse rotating multiple cross type impellers with four delta blades (CDs) were experimentally investigated in comparison with that in a baffled vessel agitated by steadily unidirectionally rotating disk turbine impellers (DTs). For the two modes of operation, the mixing time in the vessel agitated by dual impellers whose arrangement was based on the data of power consumption was larger than that in the vessel with a liquid height-to-diameter ratio of 1 agitated by single impeller. In the vessel with forward-reverse rotating multiple CDs, the mixing time decreased with the number of impellers, contrary to that in the vessel with unidirectionally rotating DTs. Decreased mixing characteristics in the deep vessel were improved by increasing the number of impellers when forward-reverse rotating CDs were used in multiple fashion.

#### NOMENCLATURE

- $C_b$  = off-bottom clearance of the lowest impeller, m
  - $C_i$  = clearance of impellers, m
  - $D_i$  = impeller diameter, m
  - $D_t$  = vessel diameter, m
  - $n_i$  = number of impellers, -
  - $N_m$  = dimensionless mixing time of liquid phase, -
  - $N_{m1}$  = dimensionless mixing time of liquid phase in single impeller system, -
  - $N_{m2}$  = dimensionless mixing time of liquid phase in dual impeller system, -
  - $N_{mm}$  = dimensionless mixing time of liquid phase in multiple impeller system, -
  - $N_p$  = impeller power number, -
  - $N_{p1}$  = impeller power number in single impeller system, -
  - $N_{p2}$  = impeller power number in dual impeller system, -
  - $N_{pn}$  = impeller power number in multiple impeller system, -
  - $N_r$  = rotation rate of impeller,  $s^{-1}$
  - $P_m$  = power consumption of impeller, W
  - $T_m$  = mixing time of liquid phase, s
  - $T_{m1}$  = mixing time of liquid phase in single impeller system, s
  - $T_{m2}$  = mixing time of liquid phase in dual impeller system, s
- Greek letter**
- $\rho$  = liquid density,  $kg/m^3$

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