

# The H Lyman- $\alpha$ actinic flux in the middle atmosphere

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**Abstract.** The penetration of solar H Lyman- $\alpha$  radiation into the terrestrial middle atmosphere is studied in detail. The Lyman- $\alpha$  actinic flux is calculated with a Monte Carlo approach including multiple resonance scattering of Lyman- $\alpha$  photons within the terrestrial atmosphere and a temperature dependent absorption cross section of molecular oxygen. The dependence of the actinic flux on the temperature profile is significant for O<sub>2</sub> column densities greater than about 10<sup>24</sup> m<sup>-2</sup>. For column densities greater than about 5 · 10<sup>24</sup> m<sup>-2</sup> resonance scattering becomes important at solar zenith angles > 60°. The O(<sup>1</sup>D) quantum yield of the O<sub>2</sub> dissociation by Lyman- $\alpha$  photons is found to decrease from 0.58 in the lower thermosphere to 0.48 in the lower mesosphere. Parameterisations for Lyman- $\alpha$  actinic flux, mean O<sub>2</sub> absorption cross section and O(<sup>1</sup>D) quantum yield including temperature dependence and resonance scattering are given valid up to a O<sub>2</sub> column density of about 10<sup>25</sup> m<sup>-2</sup>.

## 1 Introduction

The solar variability has a strong spectral dependence, with greater variation in the extreme UV part of the solar spectrum. Most of this radiation cannot penetrate the mesosphere and the uppermost stratosphere through the strong absorption by molecular oxygen. By chance, the highly variable and solar EUV spectrum dominating hydrogen Lyman- $\alpha$  line at 121.6 nm coincides with a deep minimum of the O<sub>2</sub> absorption cross section. This gives Lyman- $\alpha$  photons an important role for photolysing CH<sub>4</sub>, CO<sub>2</sub>, and H<sub>2</sub>O in the mesosphere.

Within most models of the middle atmosphere the Lyman- $\alpha$  flux is parameterised by a simple exponential (e.g. Nicolet, 1984). Chabrilat and Kockarts (1997) showed that such parameterisations are not sufficient to describe the Lyman-

$\alpha$  flux in the mesosphere, because the O<sub>2</sub> absorption cross section has a temperature dependence which varies over the spectrally resolved solar Lyman- $\alpha$  line profile. They give an improved parameterisation based on a sum of exponentials of the O<sub>2</sub> (slant) column. In fact, their scheme does not include a detailed treatment of solar zenith angle dependence and the dependence of seasonal changes of the temperature profile within the mesosphere. In addition, determination of the Lyman- $\alpha$  actinic flux (which is equivalent to the photon number density) is complicated by Lyman- $\alpha$  resonant scattering in the terrestrial atmosphere, which gives rise to a prominent diffuse Lyman- $\alpha$  field.

These effects are not included in parameterisations used in models of the middle atmosphere. Calculations of the Lyman- $\alpha$  dayglow in the thermosphere have been performed by different authors (see e.g. Bishop, 1999; Bush and Chakrabarti, 1995; Meier, 1991), but those studies do not reach into the mesosphere and do not include the temperature dependence of the O<sub>2</sub> absorption. As the optical depth for Lyman- $\alpha$  absorption is high in the mesosphere, even small changes in the outer conditions may produce observable effects in the photolysis rates. The evaluation of the importance of these effects demands a detailed wavelength dependent description combining scattering and absorption processes of Lyman- $\alpha$  photons within the atmosphere. For that purpose, a Monte Carlo program (MCP) was developed which takes into account the temperature dependent absorption by molecular oxygen and multiple resonance scattering by atomic hydrogen within the terrestrial atmosphere.

## 2 Description of the method

In order to determine the path of a single photon, first its wavelength is determined randomly, according to the solar line profile. Then the altitude of absorption or scattering is determined randomly, as well as whether absorption or scat-

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tering occurs, according to the absorption coefficient of O<sub>2</sub> and the scattering coefficient of H. Resonant scattering is treated with frequency redistribution caused by the associated Doppler effect. Following Meier (1991) (page 43) the natural linewidth is neglected. In case of scattering the path of the photon is continued with a random new direction and a new wavelength. As we are mainly interested in the mesosphere, a plane parallel atmosphere is assumed. Bush and Chakrabarti (1995) compare plane parallel and spherical calculations and show that up to about 70° solar zenith angle the difference between the two methods is less than 10%, which is sufficient in the context of our study. For larger solar zenith distances the plane parallel version underestimates the contribution of scattered photons. To include resonantly scattered photons in the exosphere the outer boundary for the model is set at 1000 km. For each parallel layer the temperature and the densities of O<sub>2</sub> and H are taken from the MSIS-90 model of Hedin (1991).

In our calculations we consider 10<sup>9</sup> photons for each run. To determine the actinic flux and the photodissociation rates of O<sub>2</sub> we add the contributions of every photon along its path, using an altitude grid of 1 km resolution and a wavelength grid of 0.0004 nm resolution.

Whereas for the determination of the dissociation rates of H<sub>2</sub>O, CH<sub>4</sub> and other species the integrated actinic flux is sufficient, the O<sub>2</sub> dissociation rate is determined within the model as the integration over the Lyman- $\alpha$  spectrum. In addition, Lacoursière et al. (1999) showed that the O(<sup>1</sup>D) yield of Lyman- $\alpha$  absorption is wavelength dependent, too. The determination of this yield is also included in the MCP module.

### 2.1 Solar H Lyman- $\alpha$ emission profile

First the initial wavelength  $\lambda$  of the photon is determined randomly. We assume that the solar H Lyman- $\alpha$  spectral distribution is proportional to

$$\exp\left(-\frac{(\lambda - \lambda_0)^2}{2s_1^2}\right) \cdot \left(1 - a \exp\left(-\frac{(\lambda - \lambda_0)^2}{2s_2^2}\right)\right)$$

(self-reversed Gaussian profile) with  $\lambda_0 = 121.567$  nm,  $s_1 = 0.0248$  nm,  $s_2 = 0.0172$  nm,  $a = 0.7153$ , according to Scherer et al. (2000) (standard case, see their Fig. 2). Thus  $\lambda$  may be determined by the Neumann's rejection method: Pick random numbers Ran to calculate

$$\lambda = \lambda_0 + s_1 \cos(2\pi \text{Ran}) \sqrt{-2 \ln \text{Ran}} \quad (1)$$

again and again until

$$\text{Ran} > a \exp\left(-\frac{(\lambda - \lambda_0)^2}{2s_2^2}\right)$$

is satisfied. Here and in the following, all Rans denote random numbers realising (different) independent real random

variables with a uniform distribution on [0, 1]. Note that formula (1) alone would yield the Gaussian distribution with standard deviation  $s_1$ , according to the method of Box and Muller (1958).

Now the photon with the just calculated wavelength  $\lambda$  enters the top of the atmosphere. The angle of incidence is the solar zenith angle  $\chi$ .

### 2.2 Extinction of the photon

We assume that the photon now starts in general at some altitude  $z$  with some wavelength  $\lambda$  and with some angle  $\phi$  (between 0 and 180°) to the downward directed vertical line.

Then the coefficients for scattering, absorption, extinction, i.e.  $\alpha_H$ ,  $\alpha_{O_2}$ ,  $\alpha_0 = \alpha_H + \alpha_{O_2}$ , are calculated for the current wavelength  $\lambda$  at the grid altitude  $z_0$  within the layer in which the photon just moves. For atomic hydrogen we use the scattering cross section

$$\sigma_H = \frac{f_{12} \mu_0 e^2 \lambda_0^2}{4\sqrt{\pi} m_e \Delta\lambda_D} \exp\left(-\left(\frac{\lambda - \lambda_0}{\Delta\lambda_D}\right)^2\right)$$

(in SI units) with the absorption oscillator strength  $f_{12} = 0.4163$  and the Doppler width  $\Delta\lambda_D = \lambda_0 v_{th}/c$  where  $v_{th} = \sqrt{2kT/m_H}$  denotes the thermal velocity. The absorption cross section  $\sigma_{O_2}$  of molecular oxygen is taken from Lewis et al. (1983) by interpolation.

For simplicity the extinction coefficient  $\alpha$  is assumed to vary exponentially with respect to the altitude  $z'$  in the current layer, i.e.  $\alpha = \alpha_0 e^{-\gamma(z'-z_0)}$  where  $\gamma$  is assessed by the extinction coefficients of the two surrounding layers. Then the probability  $p'$ , that the photon will reach any given altitude  $z'$  within the layer on the ray, satisfies  $dp'/dz' = \alpha p'/\cos\phi$ . Since  $p' = 1$  for  $z' = z$ , we conclude

$$\ln p' = -\frac{\alpha_0}{\gamma \cos\phi} \left(e^{-\gamma(z'-z_0)} - e^{-\gamma(z-z_0)}\right).$$

Thus the photon is absorbed or scattered at an altitude  $z_{new}$  which may be calculated for the moment by

$$z_{new} = z_0 - \frac{1}{\gamma} \ln \left( e^{-\gamma(z-z_0)} - \frac{\gamma \cos\phi}{\alpha_0} \ln \text{Ran} \right)$$

if the argument of the outer logarithm is positive, otherwise  $z_{new}$  is taken as  $\pm\infty$  with the same sign as  $\gamma$ . But if this  $z_{new}$  would lie outside of the current layer, then the photon is restarted with  $z$  at the boundary of the layer, and all the computations above are made with the adjacent layer, unless the photon escapes from the atmosphere.

When the photon is actually absorbed or scattered, the actinic flux in every layer between  $z$  and  $z_{new}$  is increased by an amount proportional to the length of the particular section on the ray.

Finally, at the current place of extinction, the photon is absorbed by some O<sub>2</sub> molecule if the inequality  $\text{Ran} < \alpha_{O_2}/\alpha_0$  holds. In that case the O<sub>2</sub> molecule is photodissociated, and

the photodissociation rate of O<sub>2</sub> (in the actual layer) is increased, as well as the O(<sup>1</sup>D) yield according to the expression

$$1.08 - \frac{0.168}{0.11\sqrt{2\pi}} \exp\left(-\frac{(\lambda/\text{nm} - 121.623)^2}{2 \cdot 0.11^2}\right),$$

which is given in Lacoursière et al. (1999) (for 121.46 to 121.67 nm).

### 2.3 Resonance scattering by H

We suppose now that the photon is not absorbed by O<sub>2</sub> but scattered by excitation of some H-atom.

First, the velocity  $\mathbf{v}$  of the scattering H-atom has, in local Cartesian coordinates, the component  $v_1 = -c(\lambda - \lambda_0)/\lambda_0$  in the direction of the photon before scattering. The component  $v_3$  is taken to be horizontal, whereas  $v_2$  directs to lower altitudes. These two components are calculated by  $v_2 = r \cos \psi$  and  $v_3 = r \sin \psi$  with  $r = v_{\text{th}} \sqrt{-\ln \text{Ran}}$  and  $\psi = 2\pi \text{Ran}$ , according to the Maxwellian velocity distribution and the Box-Muller method.

For the angular dependence of the intensity of resonantly scattered radiation we use the expression  $\frac{11}{12} + \frac{3}{12} \cos^2 \theta$ . This expression can be deduced from Chandrasekhar (1960) and is given explicitly for example in Cranmer (1998). Therefore the component  $n_1$  (in the previous direction) of the photon's new (normalised) direction  $\mathbf{n}$  has a probability density proportional to  $11 + 3n_1^2$  on  $[-1, 1]$ . Thus  $n_1$  may be determined by the Neumann's rejection method: Calculate  $n_1 = 2\text{Ran} - 1$  again and again until  $\text{Ran} < (11 + 3n_1^2)/14$  is satisfied. Then calculate  $n_2 = \cos \beta \sqrt{1 - n_1^2}$  and  $n_3 = \sin \beta \sqrt{1 - n_1^2}$  where  $\beta = 2\pi \text{Ran}$ .

This new direction  $\mathbf{n}$  determines the photon's new angle  $\phi_{\text{new}}$  to the vertical direction  $\mathbf{n}_{\text{ver}}$  by  $\cos \phi_{\text{new}} = \mathbf{n} \cdot \mathbf{n}_{\text{ver}} = n_1 \cos \phi + n_2 \sin \phi$ , and the photon's new wavelength  $\lambda_{\text{new}}$  by  $(\lambda_{\text{new}} - \lambda_0)/\lambda_0 = -\mathbf{n} \cdot \mathbf{v}/c$ , which implies  $\lambda_{\text{new}} = \lambda_0 - \lambda_0(n_1 v_1 + n_2 v_2 + n_3 v_3)/c$ .

Having completed one step the computation is repeated with  $z_{\text{new}}$ ,  $\lambda_{\text{new}}$ ,  $\phi_{\text{new}}$  replacing  $z$ ,  $\lambda$ ,  $\phi$ . This loop terminates when the photon is absorbed by O<sub>2</sub> or escapes from the atmosphere. Then the next photon is considered.

## 3 Results

For different climatological situations the spectral distribution of the normalised actinic flux

$$\widehat{Q} = \frac{Q}{Q_\infty}$$

has been calculated, where  $Q$  denotes the actinic flux of the Lyman- $\alpha$  line, and  $Q_\infty$  the corresponding solar flux outside the atmosphere. The  $T$ -, O<sub>2</sub>- and H-profiles for equinox and solstice conditions have been taken from the MSIS model

(Hedin, 1991) using their standard parameters for solar activity which refer to about solar mean conditions. Tests for solar maximum and minimum conditions showed only small deviations of the normalised actinic flux of less than a few percent.

### 3.1 Spectral evolution

Figure 1 shows two examples of the spectral evolution of the normalised actinic flux. One outstanding feature is the resonance peak seen at an altitude of 200 km at the line centre for solar zenith angle  $\chi = 0^\circ$ . It demonstrates the effect of resonance scattering in the terrestrial atmosphere. Lower in the atmosphere, the scattered photons having a longer path in the atmosphere are absorbed by O<sub>2</sub> with a higher probability. This causes the sharp absorption feature near the line center seen at 90 km altitude and below. The spectral dependence of O<sub>2</sub> absorption causes the asymmetry of the line shape there.

For large solar zenith angles, the spectrum already at 200 km starts with an absorption feature. This is caused in the high atmosphere by scattering photons to space. Due to the higher temperature there, this occurs in a wider spectral range. The double peaked spectrum at very low altitudes is caused by Lyman- $\alpha$  photons resonantly scattered in the high atmosphere downwards, therefore experiencing a smaller O<sub>2</sub> column density compared to the direct solar beam.

### 3.2 Actinic flux

The normalised actinic flux  $\widehat{Q}$  has been calculated by integration of the spectral distribution and is shown in Fig. 2 as a function of O<sub>2</sub> column density for combinations of date, latitude and solar zenith angle as noted. Here and in the following, always the slant column is given. For O<sub>2</sub> columns higher than  $10^{25} \text{ m}^{-2}$  the effects of scattering are clearly dominant for large solar zenith angles.

Nicolet (1985) and Chabrilat and Kockarts (1997) give approximations of the Lyman- $\alpha$  actinic flux within the mesosphere. The temperature dependence of the O<sub>2</sub> absorption coefficient is accounted for by a corrected column density or by a sum of exponentials, respectively, but only for a fixed temperature profile.

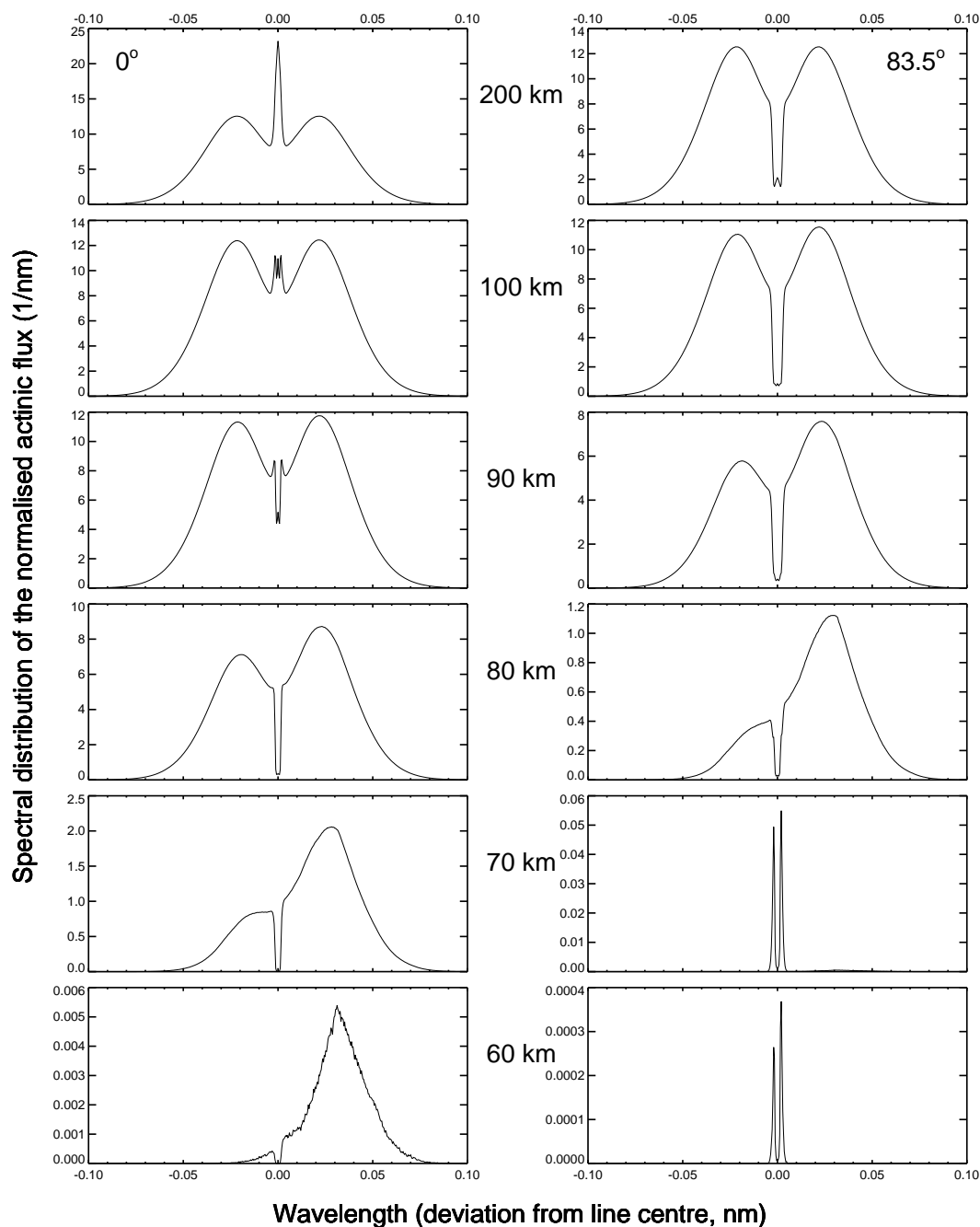
To account for different temperature profiles and in order to include the contribution of scattered photons we use the parameterisation

$$\widehat{Q} = f e^{-\bar{\tau}} + \widehat{Q}_s \quad (2)$$

with the mean optical depth

$$\begin{aligned} \bar{\tau} = & (2.48 \cdot 10^{-22} + 6 \cdot 10^{-26} \text{ K}^{-1} T_1) (\text{m}^2 N)^{0.9} \\ & - (2.6 \cdot 10^{-25} - 10^{-27} \text{ K}^{-1} T_2) \text{m}^2 N \\ & + 2.5 \cdot 10^{-51} \text{ m}^4 N^2 \end{aligned}$$

depending on the O<sub>2</sub> (slant) column density  $N$ , essentially.  $T_1$  and  $T_2$  denote the temperature where the O<sub>2</sub> column den-



**Fig. 1.** Spectral evolution of the Lyman- $\alpha$  line for different altitudes at solar zenith angles  $\chi = 0^\circ$  (left) and  $\chi = 83.5^\circ$  (right). Integral over the solar line is set to 1. Note the different scales.

sity is  $N_1 = 10^{24} \text{ m}^{-2}$  or  $N_2 = 6 \cdot 10^{24} \text{ m}^{-2}$ , respectively. The factor

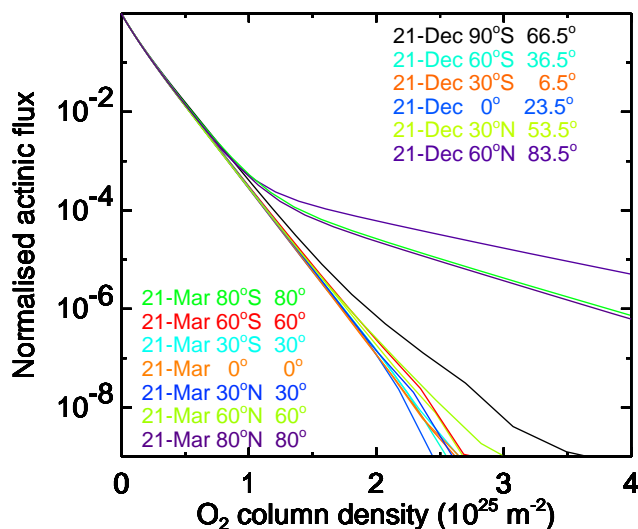
$$f = 1 + 0.07 (\cos \chi - 0.5) \exp(-4 \cdot 10^{-24} \text{ m}^2 N)$$

gives the variations with respect to the solar zenith angle  $\chi$  at low  $\text{O}_2$  column densities. The addend

$$\hat{Q}_s = 0.005 (\cos \chi + 0.07) \cdot \exp(-9.8 \cdot 10^{-25} \text{ m}^2 N (\cos \chi + 0.02))$$

gives the contribution of scattering for larger solar zenith angles at high  $\text{O}_2$  column densities.

Figure 3 shows the comparison of the MCP results with the parameterisation for the set of combinations of date, latitude and solar zenith angle as given, together with the specific temperature profiles. Up to a column density of  $\text{O}_2$  of about  $10^{25} \text{ m}^{-2}$  the deviations between exact and approximate solution are less than 5%. In addition, the parameterisation of



**Fig. 2.** Normalised actinic flux  $\hat{Q}$  of the Lyman- $\alpha$  line as a function of  $O_2$  (slant) column for different combinations of date, latitude and solar zenith angle, calculated by the MCP.

Chabrillat and Kockarts (1997) is shown in Fig. 3 for comparison. For small  $O_2$  columns the effect of resonance scattering is less than about 5%, whereas the influence of different temperature profiles exceeds 5% above  $2 \cdot 10^{24} \text{ m}^{-2}$  for cases where the temperature deviates from standard conditions. Further tests show that the parameterisation gives results within 20% compared with the MCP results for attenuations  $> 10^{-6}$  for the cases studied.

### 3.3 $O_2$ photodissociation

Figure 4 shows the normalised  $O_2$  photodissociation rate

$$\hat{J}_{O_2} = \frac{J_{O_2}}{Q_\infty}$$

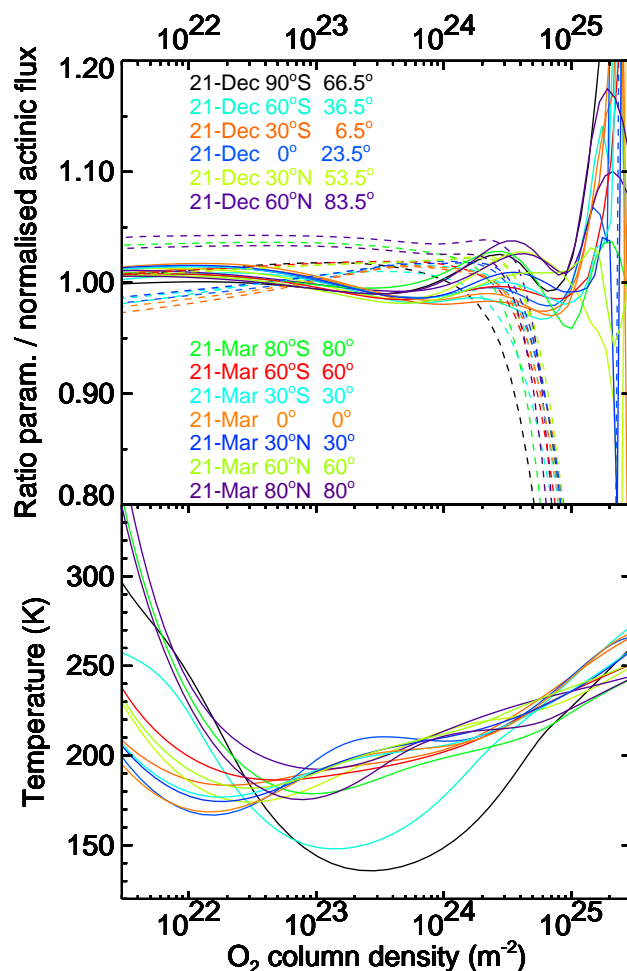
as a function of altitude for different cases, calculated by the Monte Carlo program. The mean  $O_2$  absorption cross section defined by

$$\bar{\sigma}_{O_2} = \frac{J_{O_2}}{n_{O_2} Q} = \frac{\hat{J}_{O_2}}{n_{O_2} \hat{Q}}$$

is shown in Fig. 5. It can be approximated by the parameterisation

$$\begin{aligned} \bar{\sigma}_{O_2} = & 0.765 \cdot 10^{-24} \text{ m}^2 \cdot (1 + 0.35 \exp(-5 \cdot 10^{-25} \text{ m}^2 N)) \\ & \cdot (1.1 + 0.1 \tanh(3 \cdot 10^{-25} \text{ m}^2 N (0.8 - \cos \chi)^+ - 2.4)) \\ & \cdot (1.16 - 0.0021 \text{ K}^{-1} T + 6 \cdot 10^{-6} \text{ K}^{-2} T^2) \end{aligned} \quad (3)$$

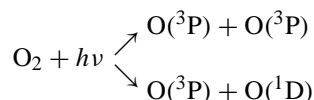
with the function  $x^+ = \max(x, 0)$ . For comparison in Fig. 6 the ratio of this parameterisation to the mean  $O_2$  absorption cross section  $\bar{\sigma}_{O_2}$  derived from the MCP results is shown.



**Fig. 3.** Comparison of the MCP results for the normalised actinic flux  $\hat{Q}$  with the parameterisation Eq. (2). Dotted lines refer to the parameterisation of Chabrillat and Kockarts (1997). Below the corresponding temperature profiles are shown.

### 3.4 Yield of $O(^1D)$

The dissociation of  $O_2$  has the form



Lacoursière et al. (1999) showed that the  $O(^1D)$  quantum yield of Lyman- $\alpha$  photons absorption strongly varies over the absorption feature near the Lyman line. It decreases from 1 shortward of the absorption feature, to less than 0.5 at the feature center and rises again to 0.7 at longer wavelengths. As the spectral form of the Lyman- $\alpha$  line changes with height within the atmosphere (see Sect. 3.1) the  $O(^1D)$  yield is also height dependent. The corresponding mean  $O(^1D)$  quantum yield  $\bar{\Phi}_{O(^1D)}$  for the whole line, which is defined as the relative frequency of the channel yielding  $O(^1D)$ , is given in

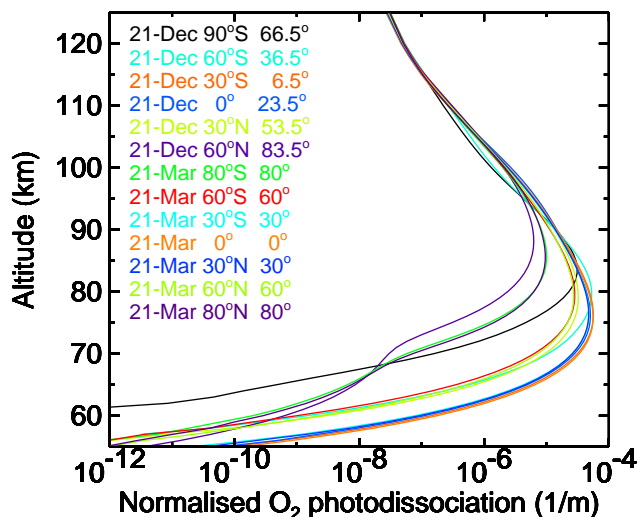


Fig. 4. Normalised O<sub>2</sub> photodissociation rate  $\hat{J}_{O_2}$  as a function of geometric altitude for different combinations of date, latitude and solar zenith angle, calculated by the MCP.

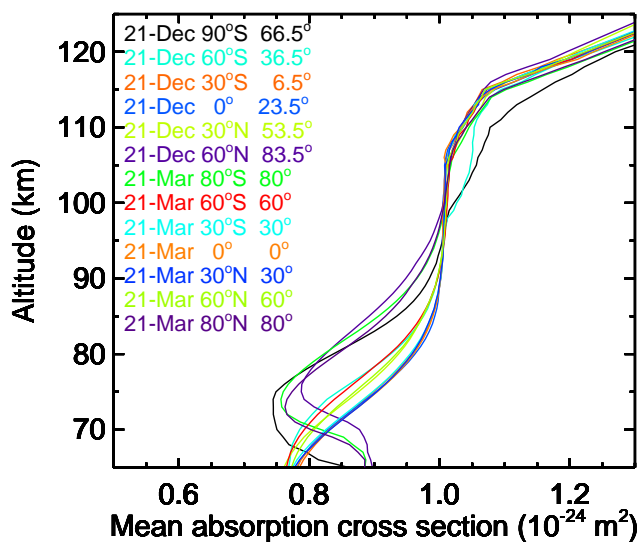


Fig. 5. Mean absorption cross section  $\bar{\sigma}_{O_2}$  as a function of altitude.

Fig. 7 for different atmospheric situations. It is 0.58 in the lower thermosphere and decreases to 0.48 in the lower mesosphere. For large solar zenith angles it increases again to 0.54, which is caused by resonantly scattered photons near the Lyman- $\alpha$  line center.

$\bar{\Phi}_{O(^1D)}$  can be parameterised in that region by the expression

$$\bar{\Phi}_{O(^1D)} = 0.48 \left( 1 + 0.2 \exp(-3 \cdot 10^{-25} \text{ m}^2 N) \right) \cdot (1.06 + 0.06 \tanh(3.5 \cdot 10^{-25} \text{ m}^2 N (0.8 - \cos \chi)^+ - 2.4))$$

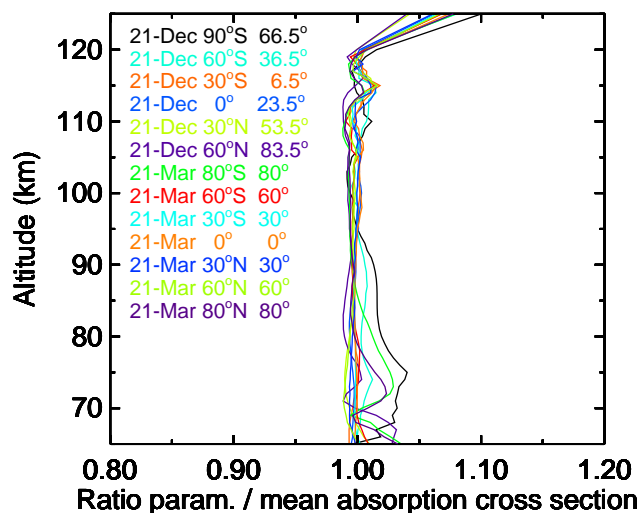


Fig. 6. Comparison of the MCP results for the mean absorption cross section  $\bar{\sigma}_{O_2}$  with the parameterisation Eq. (3).

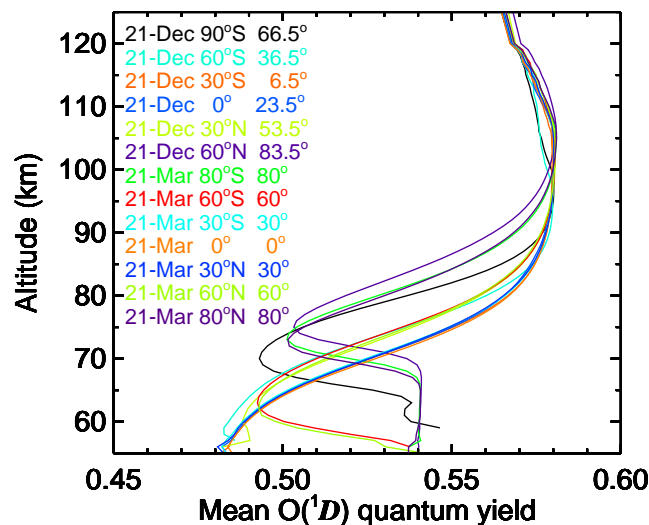


Fig. 7. Mean O(<sup>1</sup>D) quantum yield  $\bar{\Phi}_{O(^1D)}$  as a function of altitude, calculated by the MCP.

#### 4 Conclusions

Two effects influencing the actinic flux at the H Lyman- $\alpha$  line in the middle atmosphere have been studied in our analysis: First, the variation of the temperature profile causes significant changes of the solar H Lyman- $\alpha$  actinic flux for O<sub>2</sub> columns greater than about 10<sup>24</sup> m<sup>-2</sup>. Parameterisations of the actinic flux for such high O<sub>2</sub> columns should include corrections for the actual temperature profile. We remark that even for a fixed profile there is a change of the temperature as a function of column by the varying solar zenith angle. The second effect on the actinic flux studied is resonance scatter-

ing. It can be separated in two spatial regimes: for low  $O_2$  column densities ( $< 10^{23} \text{ m}^{-2}$ ) the actinic flux decreases by about 7% from small to large solar zenith angles. For high column densities ( $> 5 \cdot 10^{24} \text{ m}^{-2}$ ) and solar zenith angles  $> 60^\circ$  the actinic flux is increased by resonance scattering compared to the case without scattering. For very large solar zenith angles actinic flux is even dominated by scattered photons at column densities  $> 10^{25} \text{ m}^{-2}$ . Our new parameterisation includes both effects and agrees with the MCP result within 5% up to  $10^{25} \text{ m}^{-2}$ , but using plane parallel geometry the actinic flux for very large solar zenith angles is possibly underestimated. Chabrilat and Kockarts (1997) claim for their parameterisation an accuracy better than 2% up to  $10^{25} \text{ m}^{-2}$ . This statement neglects the influence of different temperature profiles and resonance scattering.

There are additional factors influencing the actinic flux. The shape of the solar Lyman- $\alpha$  line shape is known to change with the solar cycle (Vidal-Madjar, 1975). Especially the primary central depression may depend on solar activity, as does a slight asymmetry of the line. Both effects can be included in our program, but as reliable data are missing, this influence has been neglected in our study. In addition, but not so important, as the temperature and hydrogen density in the thermosphere and exosphere depend on solar activity, so does the exact contribution of scattered radiation.

From a chemical point of view, resonantly scattered photons may have effects especially for the concentration of  $CH_4$  which is mainly destroyed by Lyman- $\alpha$  photons. In addition, during daylight conditions the  $O(^1D)$  concentration may be affected in the mesosphere. Hence, variations in the  $O(^1D)$  yield should be considered in photochemical calculations. By implementation of our parameterisation in chemical models of the upper stratosphere and mesosphere this can be tested.

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